## EDISP 2005/2006 – Final exam, 1st approach, version A 28.01.2006



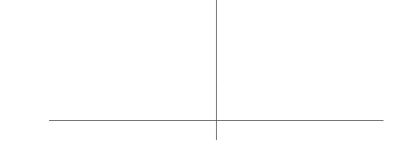
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For the short problems, try to write the answer in the provided space. Put your calculations on additional sheet. Solve long problems on the additional sheet, marked with your name.

1. A DT system is described as follows:

$$T(x[n]) = \frac{3}{2}x[n-1] + \frac{3}{2}x[n+2]$$

- (a) (2 p.) is T
- (c) (2 p.) find the step response .....
- 2. (6 p.) Let x[n] be a signal obtained by sampling a continuous-time sine wave of 10 kHz frequency with sampling period of 10  $\mu$ s
  - (a) Calculate the period K and normalized angular frequency  $\theta$  of the x[n].
  - (b) Sketch the absolute value of DFT X(k) for the transform size equal to K.
  - (c) Label the frequency axes carefully with index k and with  $\theta$  values.



- 3. (10 p.) A causal FIR filter is described by its zeros:  $z_1 = +0.5j$ ,  $z_2 = -0.5j$ . We know that the DC gain is equal to 1. and the location of zeros determines the frequency characteristics of the filter.
  - (a) Find the transfer function H(z) of the filter
  - (b) Write the difference equation for the filter.
  - (c) Sketch the graph of a simple implementation of the filter
  - (d) Find the output for a discrete input signal defined as  $x(n) = 1 + (-1)^n$
  - (e) Find the output for a discrete input signal defined as  $x(n) = \delta(n-5)$

- 4. A <u>causal</u> lowpass FIR filter of the order 7 was designed from windowed Inverse Fourier Transform of the zero-phase ideal filter characteristics. A rectangular window was used. Ideal filter cutoff was at  $\theta_b = \frac{\pi}{4}$ .
  - (a) (2 p.) Plot the phase characteristics of the resulting filter. Find the group delay.
  - (b) (3 p.) Sketch the amplitude characteristics of the resulting filter. Show and name the artefacts from the method nonideality.
- 5. "Tricky questions": to obtain a full score, remember to present your reasoning.
  - (a) (3 p.) What is the difference between DCT and DFT?
  - (b) (3 p.) A filter y(n) = x(n) + x(n-1) (x-input, y-output) filters a white noise signal  $\xi(n)$  with zero mean and standard deviation  $\sigma_{\xi} = 1$ . Sketch the PSD of the input signal  $\xi(n)$  and output signal  $\eta(n)$ .

- (c) \*(5 p.)A Bartlett window of length 2N-1 is a convolution of two rectangular windows of length N. Calculate the approximate mainlobe width of the Bartlett window. Answer: aclculation: .....
- (d) (3 p.) Why does a digital signal processor need three separate memory banks? Answer:....
- (e) (3 p.) What is the minimum width of a transition band in an LP FIR filter of order K = 8 designed with window method? Answer:  $\square$  calculation: ....
- (f) (3 p.) How do we reconstruct a signal from its DFT coefficients X(k)? Describe the difference between the periodic and finite-time signal assumption.
- (h) (5 p.) A CT signal x(t) has been sampled with the sampling frequency of 64 kHz. The 32-point FFT X(k) of the resulting signal x(n) is all zeros, except X(2) = 1. What are the possible values of the frequency of x(t) if we know that:
- (i) (3 p.) How many nonzero samples may be (at max) in the output of a 10-th order FIR filter when the input signal has 20 non-zero samples?
  Answer: all calculation: .....

