EDISP	2005	/2006 -	Final	exam	1st	anr	oroach	version	\mathbf{B}	28 01 20	006
וטוטו	4000	/ 4000 -	rmai	cam,	150	app	moach,	ACTURION	ப	40.01.40	JUU

		1
	2	
Name:	3	
Name	4	
	5	

1 |

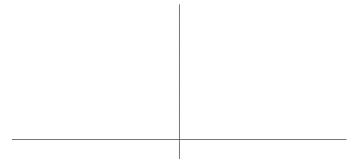
For the short problems, try to write the answer in the provided space. Put your calculations on additional sheet. Solve long problems on the additional sheet, marked with your name.

1. A DT system is described as follows:

$$T(x[n]) = \frac{3}{2}x[n-1] - \frac{3}{2}x[n-2]$$

(a) (2 p.) is T

- stable yes: or no: explain why:....
- causal yes: or no: explain why:....
- (b) (2 p.) find the impulse respone of the system T
- (c) (2 p.) find the step response
- 2. (6 p.) Let x[n] be a signal obtained by sampling a continuous-time sine wave of 0.2 ms period with sampling frequency of 100 kHz
 - (a) Calculate the period K and normalized angular frequency θ of the x[n].
 - (b) Sketch the absolute value of DFT X(k) for the transform size equal to K.
 - (c) Label the frequency axes carefully with index k and with θ values.



- 3. (10 p.) A causal FIR filter is described by its zeros: $z_1 = +0.7j$, $z_2 = -0.7j$. We know that the DC gain is equal to 1. and the location of zeros determines the frequency characteristics of the filter.
 - (a) Find the transfer function H(z) of the filter
 - (b) Write the difference equation for the filter.
 - (c) Sketch the graph of a simple implementation of the filter
 - (d) Find the output for a discrete input signal defined as $x(n) = 1 + (-1)^n$
 - (e) Find the output for a discrete input signal defined as $x(n) = \delta(n-5)$

	A <u>causal</u> lowpass FIR filter of the order 5 was designed from windowed Inverse Fourier Transform of the zero-phase ideal filter characteristics. A rectangular window was used. Ideal filter cutoff was at $\theta_b = \frac{3\pi}{4}$.							
	(a)	(2 p.) Plot the phase characteristics of the resulting filter. Find the group delay.						
		(3 p.) Sketch the amplitude characteristics of the resulting filter. Show and name the artefacts from the method nonideality.						
5.	"Tri	cky questions": to obtain a full score, remember to present your reasoning.						
	(a)	a) (3 p.) What is the difference between DCT and DFT?						
	(b)	(3 p.) A filter $y(n) = x(n) - x(n-1)$ (x-input, y-output) filters a white noise signal $\xi(n)$ with zero mean and standard deviation $\sigma_{\xi} = 1$. Sketch the PSD of the input signal $\xi(n)$ and output signal $\eta(n)$.						
	(c)	*(5 p.)A Bartlett window of length $2N-1$ is a convolution of two rectangular windows of length N . Calculate the approximate mainlobe width of the Bartlett window. Answer: \square calculation:						
	(d)	(3 p.) Why does a digital signal processor need three separate memory banks? Answer:						
	(e)	(3 p.) What is the minimum width of a transition band in an LP FIR filter of order $K=8$ designed with window method? Answer: \square calculation:						
	(f)	(3 p.) How do we reconstruct a signal from its DFT coefficients $X(k)$? Describe the difference between the periodic and finite-time signal assumption.						
	(g)	(4 p.) How many complex number multiplications do we need to compute a 2-dimensional DFT of a 2D finite-time signal of NxN samples, using the definition formula (not the FFT method). Answer: calculation:						
	(h)	(5 p.) A CT signal $x(t)$ has been sampled with the sampling frequency of 64 kHz. The 32-point FFT $X(k)$ of the resulting signal $x(n)$ is all zeros, except $X(2) = 1$. What are the possible values of the frequency of $x(t)$ if we know that:						
		i. a good antialiasing filter was used (Answer:						
		ii. an antialiasing filter was not used (Answer:)						
	(i)	(3 p.) How many nonzero samples may be (at max) in the output of a 10-th order FIR filter when the input signal has 20 non-zero samples? Answer: calculation:						