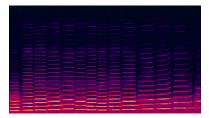
EDISP (Inst. Spectrum - STFT )
(English) Digital Signal Processing
Instantaneous spectrum
or
Short Time Fourier Transform lecture

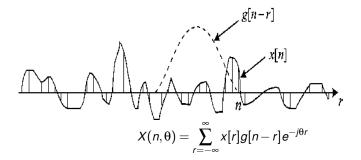
November 2, 2009

### Signal properties changing in time

- FT/DFT etc: signal properties assumed constant in a whole analysis time
- True signals (e.g. speech, music, video): main information content in the changes of the signal properties
- (A simple idea) how to analyse such signals:
  - get a small section of a signal
  - assume properties stable inside section
  - analyze section (calculate spectrum)
  - move to next section (and repeat the procedure)
  - ► Finally draw a 2d-picture (abs() spectrum vs. time) → spectrogram



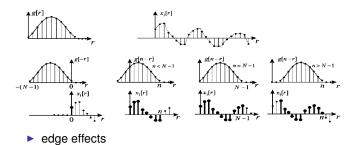
#### Formulation



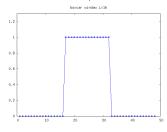
- A window g(n) of length L is non-zero if n = 0, 1, ..., L-1 (beware others may define symmetrical windows)
- ▶ so n in  $X(n, \theta)$  is the *end* of window
- ▶ The result depends on *L* and window type (recall windows lecture)

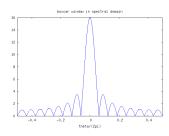
# Sliding a window

resolution



#### Can't have both :-)

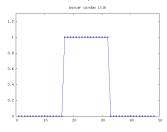


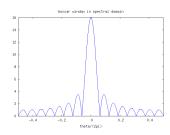


- ▶ Resolution in time ≈ L (window length)
- Resolution in frequency  $\approx \frac{4\pi}{L}$
- And we also want low sidelobes (= "good" windows)
- good windows are bad windows



#### Can't have both :-)

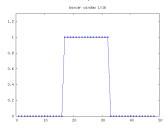


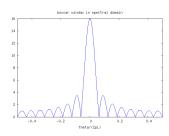


- ▶ Resolution in time  $\approx L$  (window length)
- Resolution in frequency  $\approx \frac{4\pi}{L}$
- And we also want low sidelobes (= "good" windows)
- good windows (with low sidelobes) are bad windows



#### Can't have both :-)

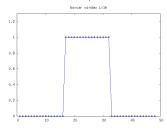


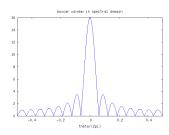


- ▶ Resolution in time ≈ L (window length)
- Resolution in frequency  $\approx \frac{4\pi}{L}$
- And we also want low sidelobes (= "good" windows)
- good windows (with low sidelobes) are bad windows (have wide mainlobe



#### Can't have both :-)





- Resolution in time  $\approx L$  (window length)
- ► Resolution in frequency  $\approx \frac{4\pi}{I}$
- ► And we also want low sidelobes (= "good" windows)
- good windows (with low sidelobes) are bad windows (have wide mainlobe and are effectively shorter in time)

### Wider view of the problem

#### Other names for the same:

- ► Short-Time Fourier Transform (STFT)
- Short-Term Fourier Transform (STFT)
- ► Time-Dependent Fourier Transform (TDFT)

Other approaches: Time-Frequency Transforms in general

- ▶ Wigner-Ville transform  $W_X(n,\theta) = \sum_{r=-\infty}^{+\infty} x(n+r)x^*(n-r)e^{-j\theta 2r}$
- Wavelet transform (use time-concentrated basis functions)
- Chirplet transform
- ...