EDISP (English) Digital Signal Processing

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General information

Lectures 2h/week, Thu, 08:15-10

Labs \approx 4h/2weeks: Monday 8:15-12, room CS203. See the schedule. (Add. dates on Fri)

First meeting for all students – 9:15, see webpage or the blackboard Labs start with an "entry test"!!!

Contact J. Misiurewicz, (jmisiure@elka.pw.edu.pl) room 454.

Web page http://staff.elka.pw.edu.pl/~jmisiure/

 \longrightarrow Slides on the evening before lecture (usually ;-))

Homeworks Announced as a preparation for the tests.

Exams Two short tests within lecture hours (see the lab schedule) and a final exam during the summer exam session (TBA).

Scoring:	2x10%	=	20%	tests
	6x5%	=	30%	lab + entry test (lab 0 – not scored)
			50%	final exam
	2x2%	=	4%	extra for homeworks (maybe even more)

Short path if $[(score \ge 41)\&\&(tests \ge 15)\&\&(test \ge 25)]$; then score* = 2; fi "if" conditions are evaluated once, before re-doing tests etc.

Books

base book The course is based on selected chapters of the book:

- A. V. Oppenheim, R. W. Schafer, *Discrete-Time Signal Processing*, Prentice-Hall 1989 (or II ed, 1999; also previous editions: *Digital Signal Processing*).
- free book A free textbook covering some of the subjects can be found here: http://www.dspguide.com/pdfbook.htm The book is slightly superficial, but nice
- **good book** Edmund Lai, *Practical Digital Signal Processing for Engineers and Technicians*, Newnes (Elsevier), 2003
- **exercise book** Vinay K. Ingle, John G. Proakis, *Digital Signal Processing using MATLAB*, Thomson 2007;*Helps understand Matlab usage in the lab (but is NOT a lab base for us)*

Additional books available in Poland:

R.G. Lyons, Wprowadzenie do cyfrowego przetwarzania sygnałów (WKiŁ 1999) Craig Marven, Gilian Ewers, Zarys cyfrowego przetwarzania sygnałów, WKiŁ 1999 [en: A simple approach to digital signal processing, Wiley & Sons, 1996] Tomasz P. Zieliński, Od teorii do cyfrowego przetwarzania sygnałów, WKiŁ 2002

You may also buy/borrow a laboratory scriptbook for a Polish language course (Cyfrowe Przetwarzanie Sygnałów, red. A Wojtkiewicz, Wydawnictwa PW) – but our lab is different!

A schedule was here - see the webpage for an updated version!

Course aims or what I will check when it comes to grading

- knowing the mathematical fundamentals of discrete-time (DT) signal processing: DT signals, normalized frequency notion, DT systems, LTI assumption, impulse response, stability of a system
- understanding the DT Fourier transforms and know how to apply them to simple DT signal analysis
- knowing basic window types and their usage for FT and STFT
- understanding the description of a DT system with a graph, difference equation, transfer function, impulse response, frequency response
- being able to apply Z-transform in analysis of a simple DT system
- understanding filtering operation and the process of DT filter design; being able to use computer tools for this task
- knowing the basic ways of implementing DSP algorithms (with PC, signal processor, hardware FPGA)
- understanding 2D signal processing basics: 2D convolution/filtering, 2D Fourier analysis
- being able to use a numerical computer tool (Matlab, Octave or similar) for simulating, analyzing and processing of DT signals

What Is EDISP All About ;-)

Theory Discrete-time signal processing

Practice Digital signal processing

Application examples:

Filters Guitar effects, radar, software radio, medical devices... A digital filter does not lose tuning with aging, temperature, humidity...
Adaptive filters Echo canceller, noise cancellation (e.g. hands-free microphone in a car),...
Discrete Fourier Transform/FFT Signal analyzer, OFDM modulation, Doppler USG, ...
Random signals Voice compression, voice recognition....
2D signals Image processing, USG/CT/MRI image reconstruction, directional receivers, ...
Upsampling/Interpolation CD audio output,

Oversampling CD audio D/A conversion (example)

Please have a look at the black/green-board.

Notice & remember some things:

- Upsampling
- Filtering (and what happens to the signal spectrum)
- Frequency response (frequency characteristics) of a filter
- Trade-off: we simplify analog part by doing a tough job on the digital side

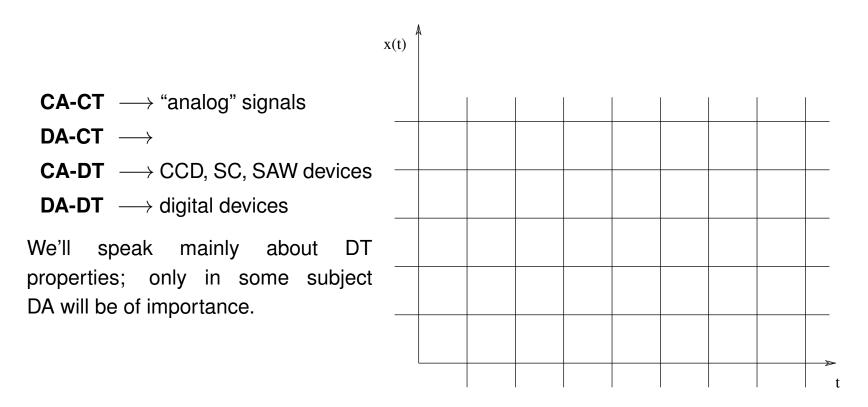
Some notes:

- First order LP filter: $A(f) = \frac{1}{\sqrt{1 + (2\pi f RC)^2}} \longrightarrow 6 \text{ dB per octave (20 dB per decade)}$
- To obtain 80 dB of attenuation we need 4 decades (10^4 times cutoff frequecy)

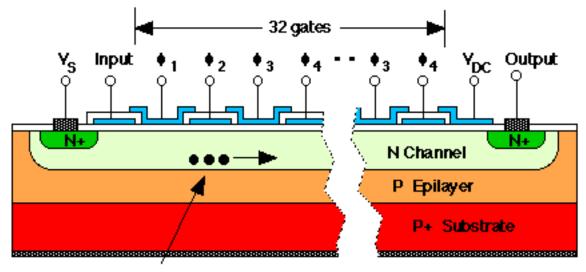
• N-th order filter:
$$A(f) = \frac{1}{\sqrt{1 + (2\pi f R C)^{2N}}}$$

Signal classes

Continuous or Discrete **amplitude** and **time**.



(side remark:) CCD device – continuous amplitude, discrete time

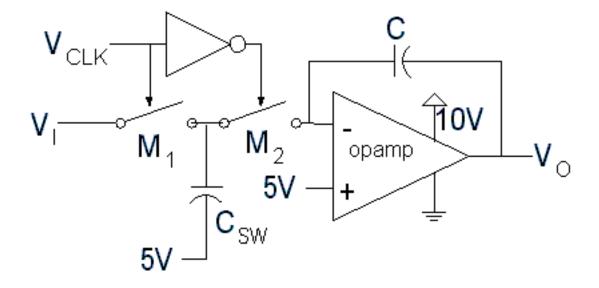


Electronpacket

Charge is transferred on the clock edge (discrete time!).

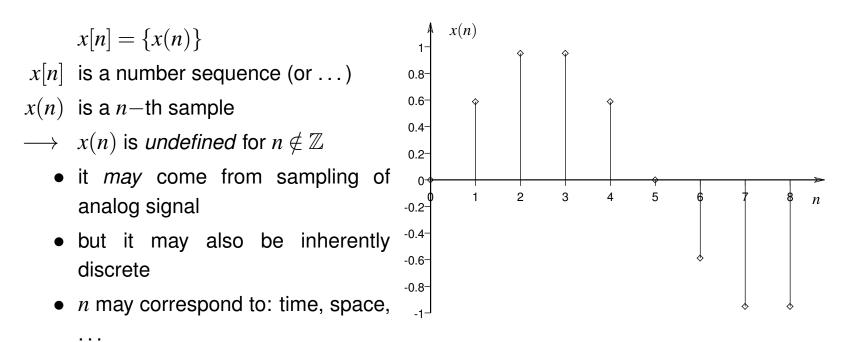
Clock is usually polyphase (2-4 phases).

SC device (another CA-DT example)



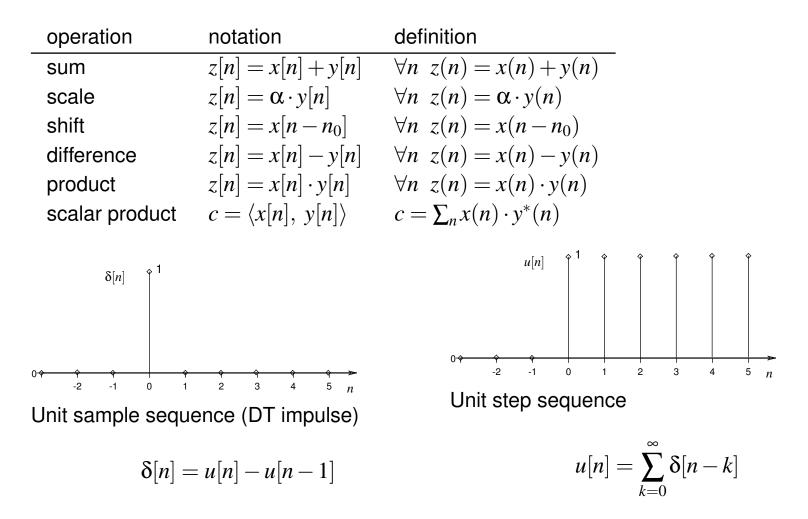
DT signal representations

DT signal \longleftrightarrow a number sequence



However, the most popular interpretation is: periodic sampling in time.

Number sequence (or DT signal) operations; basic sequences



t [ms] $n \leftarrow m \cdot T_s$ п $x(n) = x_a(nT_s)$ $n = t/T_s, T_s = 0.025 \text{ [ms]}$ $1 \overset{x(n)}{\uparrow} \overset{x(n)}{\land}$ **Misinterpretations** 0.5- \rightarrow we do not know what is between 0points 2 3 8 п a) $sin(n \cdot (1/5) \cdot \pi)$ or -0.5b) $sin(n \cdot (2+1/5) \cdot \pi)$? -1-

We have to **know** which one to choose \longrightarrow sampling theorem

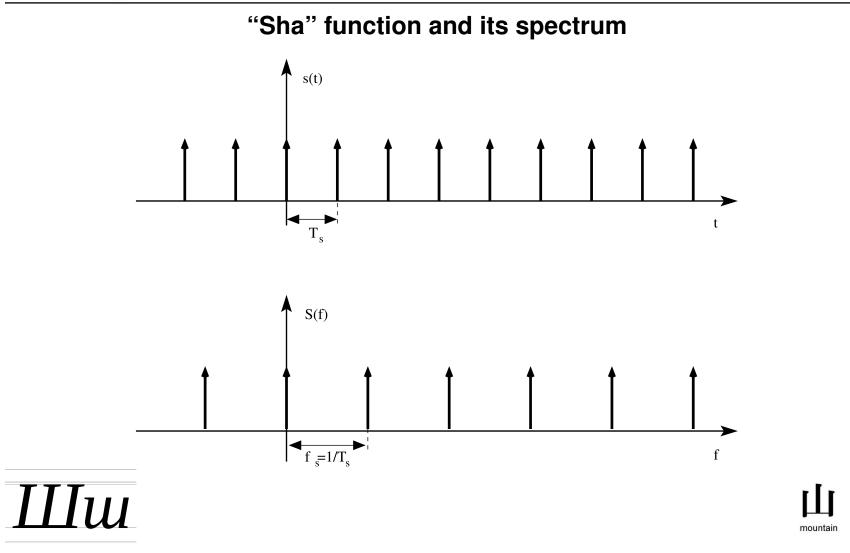
The Sampling Theorem

Named also after:

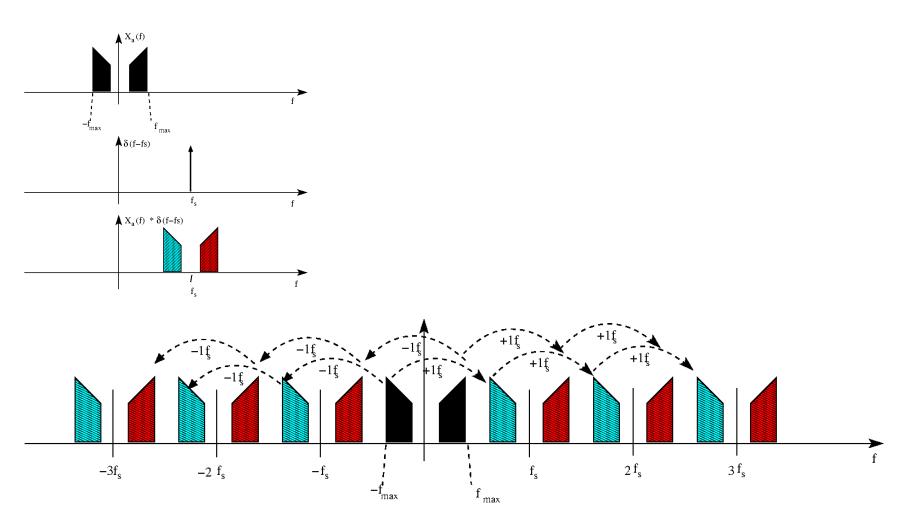
- 1915 Edmund T. Whittaker (UK)
- 1928 Harry Nyquist [ny:kvist] (SE) \longrightarrow (US)
- 1928 Karl Küpfmüller (DE)
- 1933 Vladimir A. Kotelnikov (USSR)
- 1946 Gábor Dénes (HU) → Dennis Gabor (UK)
- 1949 Claude E. Shannon (US)
- Cardinal Theorem of Interpolation Theory

If a signal is bandlimited with f_b , the reconstruction is possible from samples taken with $f_s > 2f_b$

Nyquist frequency: $f_s/2$, Nyquist rate: $2f_b$



Sampling = convolution

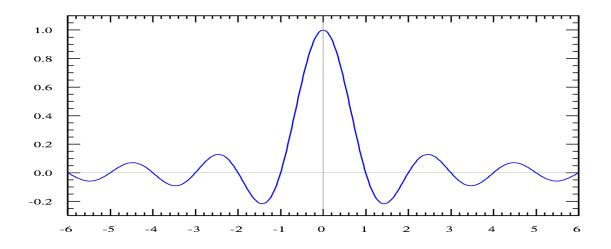


$\begin{array}{l} \textbf{Reconstruction} \\ \textbf{Reconstruction: interpolation, (sinus cardinalis sinc = Sa = } \frac{\sin(\pi x)}{\pi x} = j_0(\pi x)) \end{array}$

$$x(t) = \sum_{n = -\infty}^{\infty} x[n] \cdot \operatorname{sinc}\left(\frac{t - nT}{T}\right)$$

lowpass filtering (Küpfmüller filter) (DE)

$$x(t) = \left(\sum_{n = -\infty}^{\infty} x[n] \cdot \delta(t - nT)\right) * \operatorname{sinc}\left(\frac{t}{T}\right)$$



Sampling rates in audio processing

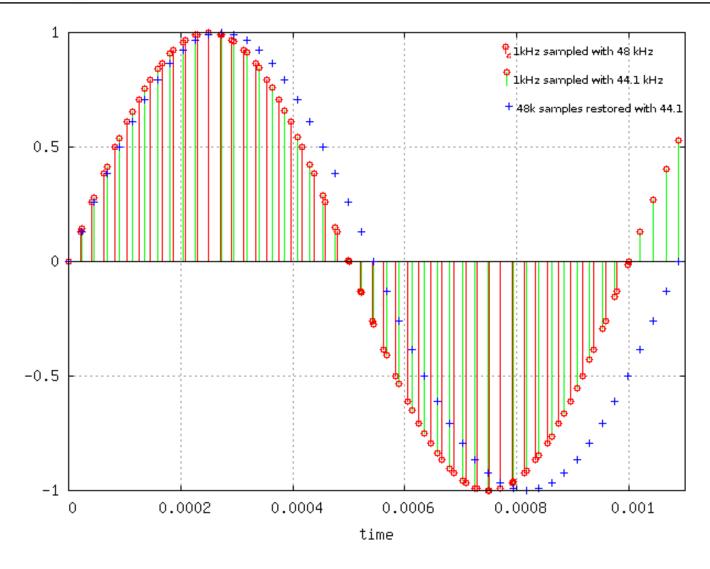
http://en.wikipedia.org/wiki/Sampling_rate
In digital audio, common sampling rates are:

- 8,000 Hz telephone, adequate for human speech
- 22,050 Hz radio
- 32,000 Hz miniDV digital video camcorder, DAT (LP mode)
- 44,100 Hz audio CD, also most commonly used with MPEG-1 audio (VCD, SVCD, MP3) compatible with PAL (625 line) and NTSC (528 line) dot frequency
- 48,000 Hz digital sound used for miniDV, digital TV, DVD, DAT, films and professional audio
- 96,000 or 192,000 Hz DVD-Audio, some LPCM DVD tracks, BD-ROM (Blu-ray Disc) audio tracks, and HD-DVD (High-Definition DVD) audio tracks
- 2.8224 MHz SACD, 1-bit sigma-delta modulation process known as Direct Stream Digital, (Sony and Philips)

Frequency in a DT signal

	CD audio system	DAT audio system
Sampling:	44100 Hz	48000 Hz
Nyquist:	22050 Hz	24000 Hz
t_s	22.676µs	20.833µs
1kHz: samples per period	44.1	48
1kHz: moved from CD to DAT	1kHz	48/44.1=1.0884 kHz

We need a good definition of frequency!



DT signal frequency concept

Continuous time cosine:		Discrete time cosine:	Normalized
$x_a(t) = \cos \omega t$	$\omega \in \mathbb{R}$	$x(n) = \cos \omega n T_s$	\ldots time: $n = t/T_s$
$\omega = 2\pi f$		$x(n) = \cos 2\pi f \ n \frac{1}{f_s}$	frequency: $f_n = \frac{f}{f_s}$
		$x(n) = \cos \theta n$	\dots ang. freq.: $\theta = 2\pi \frac{f}{f_s}$
$T = \frac{1}{f} = \frac{2\pi}{\omega}$	\leftarrow period ? \rightarrow	$N_0 = \frac{1}{f_n} = \frac{2\pi}{\Theta}$	
x(t) = x(t + kT)		x(n) = x(n+kN)	
		$x(n+N)$ defined only if $N \in \mathbb{Z}$	
Always	\leftarrow periodic \rightarrow	only if $N_0 = N/M$ (!!)	

Normalized angular frequency θ : interval of 2π may be assumed as $[0, 2\pi)$ or $[-\pi, \pi)$.

 $\cos n(\theta + k \cdot 2\pi) = \cos(n\theta + n \cdot k \cdot 2\pi) = \cos n\theta$

Normalized frequency example

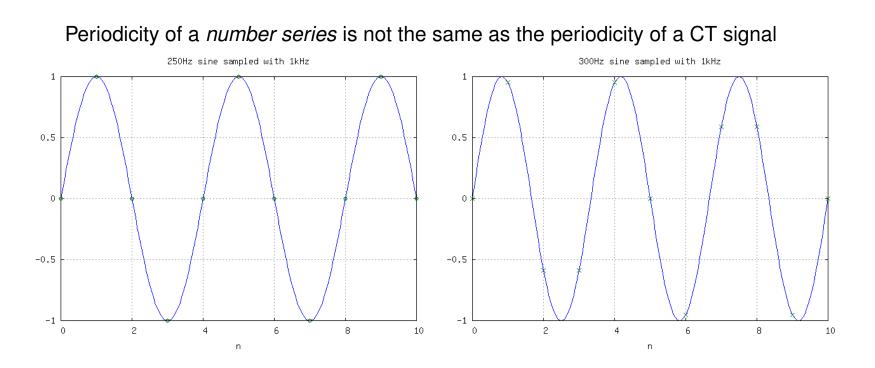
$$x_a(t) = \cos \omega t \text{ with } \omega = 1000 \cdot 2 \cdot \pi \text{ (1kHz)}$$

Let us sample it with $f_s = 48 \text{ kHz}$
 $x(n) = x_a(nT_s) = x_a(n/f_s) = \cos(1000 \cdot 2\pi \cdot n/48000) = \cos(\frac{2\pi}{48}n)$
or
 $x_a(t) = \cos \omega t \text{ with } \omega = 2000 \cdot 2 \cdot \pi \text{ (2kHz)}$
Sampled with $f_s = 96 \text{ kHz}$
 $x(n) = x_a(nT_s) = x_a(n/f_s) = \cos(2000 \cdot 2\pi \cdot n/96000) = \cos(\frac{2\pi}{48}n)$

- \rightarrow signals identical after sampling
 - Extract important parameter: $\theta = \frac{2\pi}{48}$
 - ... and we may write it down as $x(n) = \cos(\theta n)$

 \longrightarrow Normalized (angular) frequency $(2\pi) \cdot \frac{f}{f_s}$ determines the properties of the sampled signal, and now it is not important what was the frequency of x_a (only how it was related to f_s).

Periodicity example



Period of a sine wave is a real number: x(t) exists for $t \in \mathbb{R}$.

With a number series the period must be an integer, because x(n) exists only for $n \in \mathbb{Z}$.