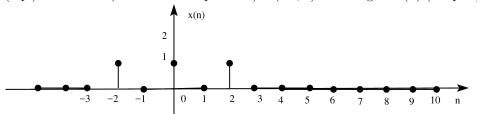
Test 2 2016l version \mathbf{B} – inst. spectrum, z-transform, filters Please mark your name and test version on all your answer pages

1. (3 p.) The STFT (instantaneous spectrum) $X(e^{j\theta}, n)$ of the signal x(n) (see plot)



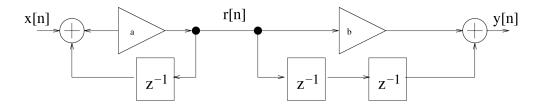
is computed using rectangular window g(k) of length K = 5.

- For n given below, sketch $|X(e^{j\theta}, n)|$ for all θ ; then calculate numerical values of $X(e^{j\theta}, n)$ at $\theta = 0, \pi/2$ and π :
 - (a) n = -3.
 - (b) n = +2.
 - (c) n = +5.

hint 1: Use the above plot to mark three positions of window.

hint 2: In one case you will look for a Fourier transform of a sum of three shifted deltas.

2. (5 p.) Analyze a filter described with the following graph:



Assume a = -9/10, b = -10/9

(a) Find H(z), h(n).

Hint: you may use r(n) as a "helper" when writing the difference equation.

- (b) Find zeros/poles and plot their location on z-plane. Check if the filter is stable
- (c) Sketch approximate $A(\theta)$
- (d) Calculate response y(n) for $x(n) = 3 + \cos(n\pi/2)$

3. (2 p.) Calculate the z-transform and determine ROC (region of convergence) for the series:

- (a) $\delta[n-2]$
- (b) $\delta[n-30] \delta[n+3]$
- (c) $u[n] \cdot (-1)^{n-3}$

4. (3 p.) A certain filter has frequency response

$$H(\theta) = \begin{cases} 1 & \text{for} & -\pi/4 < \theta < \pi/4 \\ 0 & \text{otherwise} \end{cases}$$

(a) Is the filter causal? If yes: find the group delay of the filter. If no: how to make it a causal FIR?

- (b) Calculate h(n) (find equation).
- (c) Calculate values of h(0), h(1), h(-1), h(4)

 $\Sigma=13p\ T=75\ min$