

ESPTR: Radar Basics

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Prototype



Electromagnetic version

- 1865 James Clerk Maxwell - theory of electromagnetic waves
- 1886 Heinrich Hertz - experimental proof
- 1904 Christian Hülsmeier - *Telemobiloskop*: ship collision avoidance apparatus, patented in Germany and UK; demonstration at the Rhine river in Cologne, DE.
- ...
- 1939-1945 Home Chain and other installations

Radar equation

Transmit-reflect-receive-detect

Received power: radar *range* equation

$$P_r = \frac{P_t G_t A_r \sigma F^4}{(4\pi)^2 R_t^2 R_r^2}$$

P_t transmitter power

G_t gain of the transmitting antenna

A_r effective aperture (area) of the receiving antenna

σ radar cross section, or scattering coefficient, of the target

F pattern propagation factor

R_t distance from the transmitter to the target

R_r distance from the target to the receiver.

2x range $\longrightarrow 2^4 = 16x$ power needed ...

Signal model

Transmit:

$$x_T(t) = A_T(t)e^{j\phi_T(t)}$$

Receive:

$$x_R(t) = A_T(t - R(t)/c)e^{j\phi_T(t - R(t)/c)}$$

simple case: $\phi_T(t) = \omega t + \phi_M(t)$, $R(t) = R_0 + vt$

$$x_R(t) = A_T(t - R_0/c - vt/c)e^{j(\omega(t - R_0/c - vt/c) + \phi_M(t - R_0/c - vt/c))}$$

$$x_R(t) = A_T(t - R_0/c - vt/c)e^{j(\omega t)}e^{-j\omega(R_0/c)}e^{-j\omega vt/c}e^{j\phi_M(R_0/c + vt/c)}$$

$$x_R(t) = A_T(t - R_0/c - vt/c)e^{j\phi_M(R_0/c + vt/c)}e^{j(\omega t)}e^{-j\omega(R_0/c)}e^{-j\omega vt/c}$$

Detection

Maximize P_d (detection), keep P_{fa} (false alarm) low.
The threshold set above:

- ▶ Noise (thermal etc)
- ▶ Clutter (unwanted echoes)
- ▶ Multipath
- ▶ Jamming (intentionally malicious transmitters)
- ▶ Interferences (other equipment, e.g. other radars)

Improvements: matched filter ($S\uparrow$), interference cancellation ($C\downarrow$)

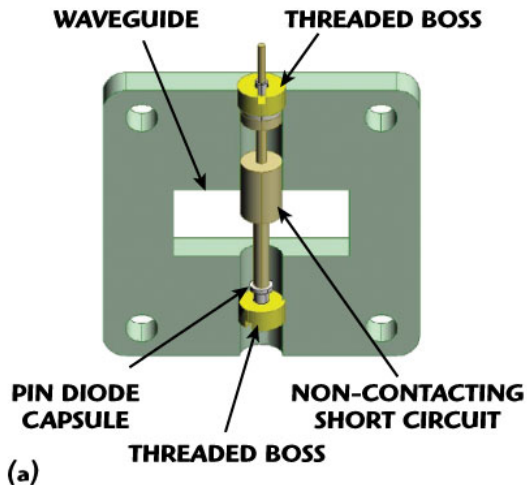
Typical: SNR ≈ 13 dB

Adaptation: CFAR

Range measurement

→ signal delay measurement

- ▶ Max *unambiguous* range limited by modulation period
- ▶ Min range limited by transmit signal entering the receiver
 - ▶ Antenna separation
 - ▶ T/R switch + receiver safety (ionised gas + pin diode)



Velocity measurement

—→ Doppler shift measurement

$$x_R(t) = A_T(t - R_0/c - vt/c) e^{j\phi_M(R_0/c + vt/c)} e^{j(\omega t)} e^{-j\omega(R_0/c)} e^{-j\omega vt/c}$$

- ▶ Min velocity: ground/meteo clutter
- ▶ Max velocity (frequency): (inverse of) modulation period

Angle measurement

- ▶ azimuth
- ▶ elevation

Methods

- ▶ Scanning: mechanical, electronic
- ▶ Monopulse techniques (multielement antenna)
 - ▶ Power ratio
 - ▶ Sigma-Delta (power)
 - ▶ Phased arrays