# ESPTR (English) Signal Processing in Telecommunications and Radar

## **Channel properties**

Jacek Misiurewicz e-mail: jmisiure@elka.pw.edu.pl

Institute of Electronic Systems Warsaw University of Technology Warsaw, Poland

#### **Communications channel**

Channel  $\longrightarrow$  (usually) everything between modulator and demodulator:

- (mainly) the transmission medium (space between antennas, or the connecting cable)
- (plus:) antennas, amplifiers, cables, waveguides, couplers, optics....

Channel properties:

- Channel bandwidth
- Channel noise
- Channel capacity
- Bandpass channel & equivalent baseband channel

#### Channel model: noise

Model: linear system + added noise; AWGN model

• Thermal noise (mainly receiver) with white PSD

$$\bar{u}_n^2 = 4k_BTR \,\mathrm{V}^2/\mathrm{Hz}$$

e.g. for room temp. and 10 kHz channel

$$P = k_B T \Delta f = 1.38 \cdot 10^{-23} \text{ J/K} \cdot 300 \text{ K} \cdot 10^4 \text{Hz} = 4.1 \cdot 10^{-17} \text{W} = -134 \text{dBm}$$

rule:  $P = -174 + 10 \log(\Delta f) [dBm]$ 

- Interfering signals (know nothing, assume white (??) → not always true!)
  - Outer space
  - Atmospheric ("static")
  - Man-made (EMC problems → computer, broken shaver motor...) impulse noise
  - Other transmissions (unintentional and ECM)

(radar only) clutter

#### **Channel model: linear**

Transmission properties

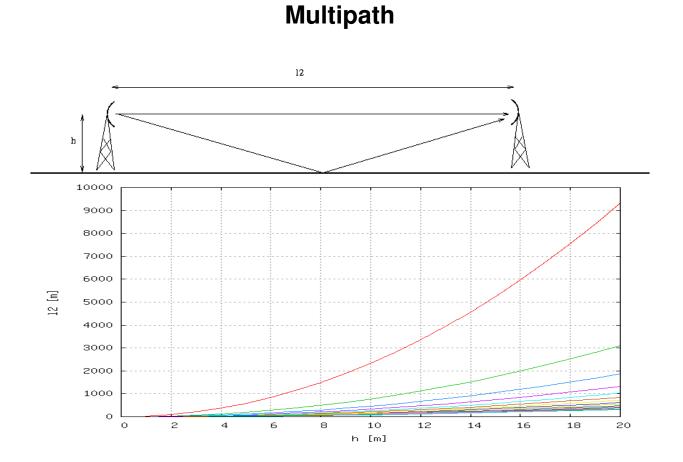
- Physical parts characteristics
- Propagation characteristics, including propagation losses  $P \sim \frac{1}{4\pi R^2}$  (one way)
- Multipath propagation  $\longrightarrow$  self-interference

Description:

- Time domain: impulse response
- Frequency domain: transfer function (phase is important!)

Non-linear:

- Doppler effect
- Impulse noise saturating the receiver



(I2=distance vs. h=tower height), 7GHz, curves for [1 3 5 .. 15]\*lambda/2, flat earth geometry

#### Effects in baseband

- Echo (ghosts on TV)
- Nonuniform frequency characteristics
- Fading in subchannels
- Fading in some regions (radar)

### **Channel capacity**

With AWGN

$$C = B\log_2\left(1 + \frac{S}{N}\right)$$

(otherwise: integrate over whole B, with S/N as a function of f, df)

#### **Doppler effect**

Transmitted signal: a band-limited envelope  $x_T(t)$  · carrier of frequency  $F_c$ 

 $X_T(t) = x_T(t) \cdot \cos(2\pi j F_c t)$ 

The received signal at  $r_0 + vt$  distance is delayed by  $t_d = \frac{r}{c} = \frac{r_0 + vt}{c}$ .

factor	Received carrier	Received envelope
$(r_0)$	phase change	delay
(v)	Doppler shift	stretch (dilation)

$$X_R(t) = A_0 \cdot X_T(t - t_d) = A_0 \cdot x_T(t - t_d) \cdot \cos(2\pi j F_c(t - t_d)) + \xi(t)$$

After the demodulation (baseband received signal):

$$x_R(t) = A_0 \cdot x_T(t-t_d) \cdot e^{-2\pi j F_c t_d}$$

or, putting  $t_d = \frac{r_0 + vt}{c}$   $A_0 \cdot x_T \left( \left(1 - \frac{v}{c}\right)t - \frac{r_0}{c} \right) \cdot e^{-2\pi j F_c \frac{r_0}{c}} \cdot e^{-2\pi j F_c \frac{vt}{c}}$ Doppler frequency  $\longrightarrow F_c \frac{v}{c}$ ; stretch factor  $\longrightarrow 1 - \frac{v}{c}$ 

### Titan calling (Doppler)

(whole story ----> IEEE Spectrum, October 2004 http://www.spectrum.ieee.org/oct04/4339/7)

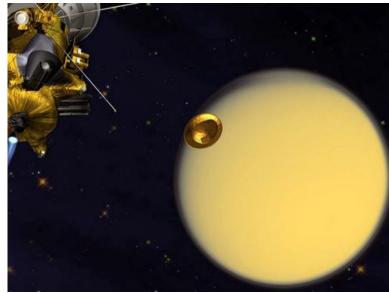
Huyghens-Cassini mission to Titan (moon of Saturn).

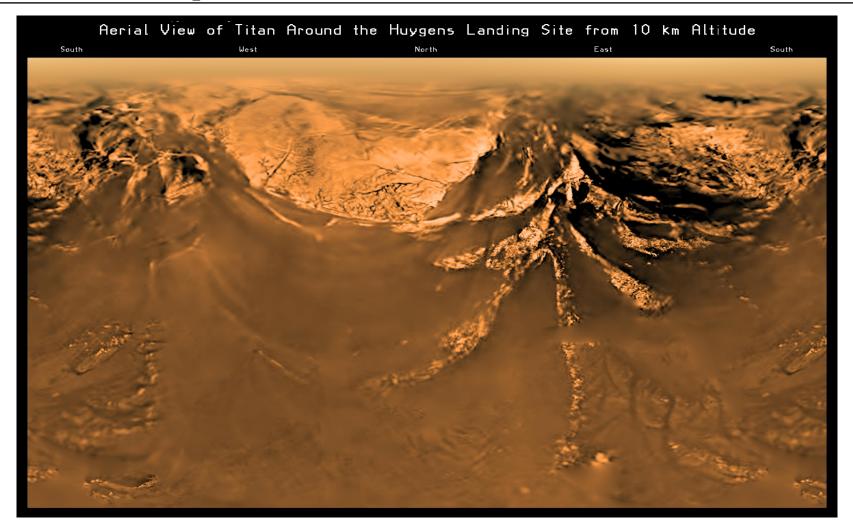
- Huyghens lander
- Cassini orbiter, retrasnmitting data to Earth
- Doppler effect on carrier frequency
- Doppler effect on data rate & sync (usually neglected, but not for spacecraft....)

(http://saturn.jpl.nasa.gov/multimedia/images/)

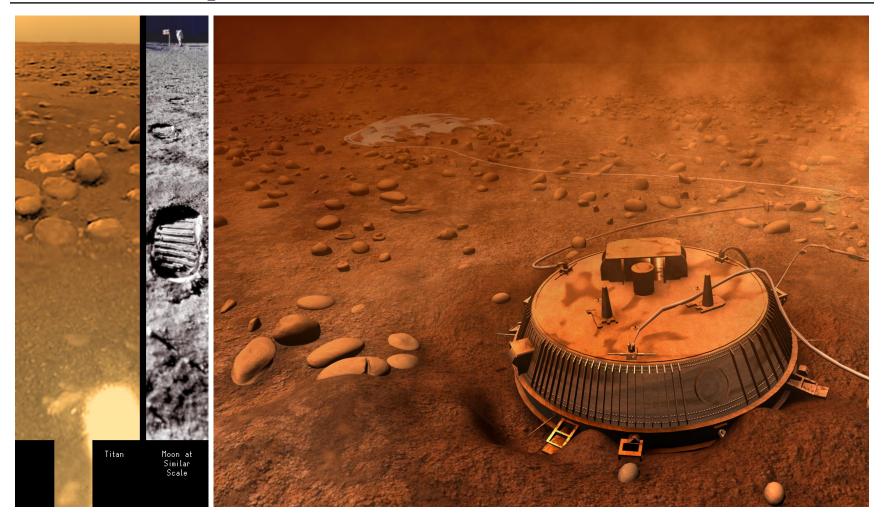
 $\longrightarrow$  solution: make Cassini orbit perpendicular to the line-of-sight

Landing: 14 January 2005





(image: http://esamultimedia.esa.int/images/cassini\_huygens/posterd\_H.jpg)



http://esamultimedia.esa.int