

ESPTR
(English)

Signal Processing in Telecommunications and Radar

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ESPTR: General information

“Credits”	2h/week lecture + 2h/week project.																	
Lecture	Thursday, 08:15-10(Possible move to Tue, 08:15-10, probably room 122) Team: dr J. Misiurewicz, mgr A. Gromek, mgr P. Krysik																	
Contact	J. Misiurewicz, (jmisiure@elka.pw.edu.pl) room 447. A web page is still expanding (http://staff.elka.pw.edu.pl/~jmisiure/esptra)																	
Projects	Simulation of a selected mechanism or technique. Two projects (“R” - Radio/Radar, due mid-term, “T” - Telecomm, due before end of term), each with two stages: 1. definition, 2. final. Environment: Matlab, Octave or NumPy, C/C++ (selected projects), other (special projects).																	
Exam	A final exam during the session																	
Scoring:	<table style="border-collapse: collapse; width: 100%;"> <tr> <td style="text-align: right; padding-right: 10px;">5%</td> <td>proj. R1: definition</td> <td></td> </tr> <tr> <td style="text-align: right; padding-right: 10px;">+ 20%</td> <td>proj. R2: final</td> <td rowspan="2">Minimum 25 pt from projects is necessary to get score > 3</td> </tr> <tr> <td style="text-align: right; padding-right: 10px;">+ 5%</td> <td>proj. T1: definition</td> </tr> <tr> <td style="text-align: right; padding-right: 10px;">+ 20%</td> <td>proj. T2: final</td> <td rowspan="3">See webpage for project deadlines and penalties for late submission.</td> </tr> <tr> <td style="text-align: right; padding-right: 10px;">= 50%</td> <td>Project total</td> </tr> <tr> <td style="text-align: right; padding-right: 10px;">= 50%</td> <td>exam</td> </tr> </table>	5%	proj. R1: definition		+ 20%	proj. R2: final	Minimum 25 pt from projects is necessary to get score > 3	+ 5%	proj. T1: definition	+ 20%	proj. T2: final	See webpage for project deadlines and penalties for late submission.	= 50%	Project total	= 50%	exam		
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Plan

- Some basics: frequency conversions, sampling&D/A, digital processing
 - Radio channel, propagation, software radio, directional reception
 - Radar basics, pulsed/CW radar, special radars
 - Digital broadcasting and reception: DAB, DVB
 - Cellular systems up to 4G/LTE, structure, modulations, receivers
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Basics: sampling

- ideal sampling
 - non-ideal sampling: model as LP filter(conv)+sampling(mul), integrating AD converter case (multimeter)
 - Nyquist sampling
 - undersampling of narrowband signals (ideal and non-ideal case)
 - reconstruction (ideal and nonideal)
 - Oversampling to ease the antialiasing filter design
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The Sampling Theorem

Named also after:

- 1915 Edmund T. Whittaker (UK)
- 1928 Harry Nyquist [ny:kvist] (SE) → (US)
- 1928 Karl Küpfmüller (DE)
- 1933 Vladimir A. Kotelnikov (USSR)
- 1946 Gábor Dénes (HU) → Dennis Gabor (UK)
- 1949 Claude E. Shannon (US)
- Cardinal Theorem of Interpolation Theory

Nyquist frequency, Nyquist rate

Sampling: bandlimited signal (aliasing problem)

Moiré pattern - as seen on TV, an example of too low sampling frequency.

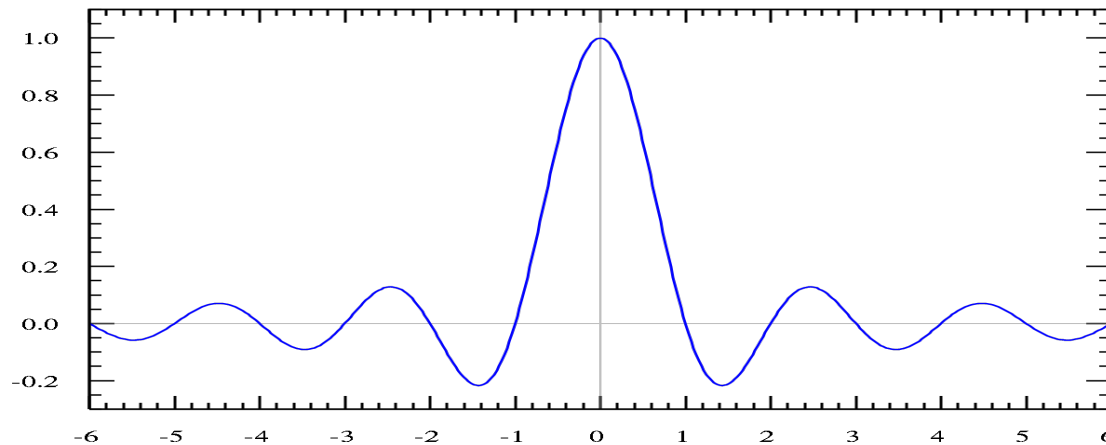
Reconstruction

Reconstruction: interpolation, (*sinus cardinalis* sinc = Sa = $\frac{\sin(\pi x)}{\pi x} = j_0(\pi x)$)

$$x(t) = \sum_{n=-\infty}^{\infty} x[n] \cdot \text{sinc}\left(\frac{t - nT}{T}\right)$$

lowpass filtering (Küpfmüller filter) (DE)

$$x(t) = \left(\sum_{n=-\infty}^{\infty} x[n] \cdot \delta(t - nT) \right) * \text{sinc}\left(\frac{t}{T}\right)$$



Bandpass sampling

(sometimes called “undersampling”)

Bandwidth less than $f_s \longrightarrow$ e.g. a signal in the band $Nf_s \pm 0.5f_s$

Antialiasing filter: bandpass!

Reconstruction: with bandpass filter!

The influence of non-ideal sampling (*system bandwidth*) \longrightarrow unwanted lowpass filter.

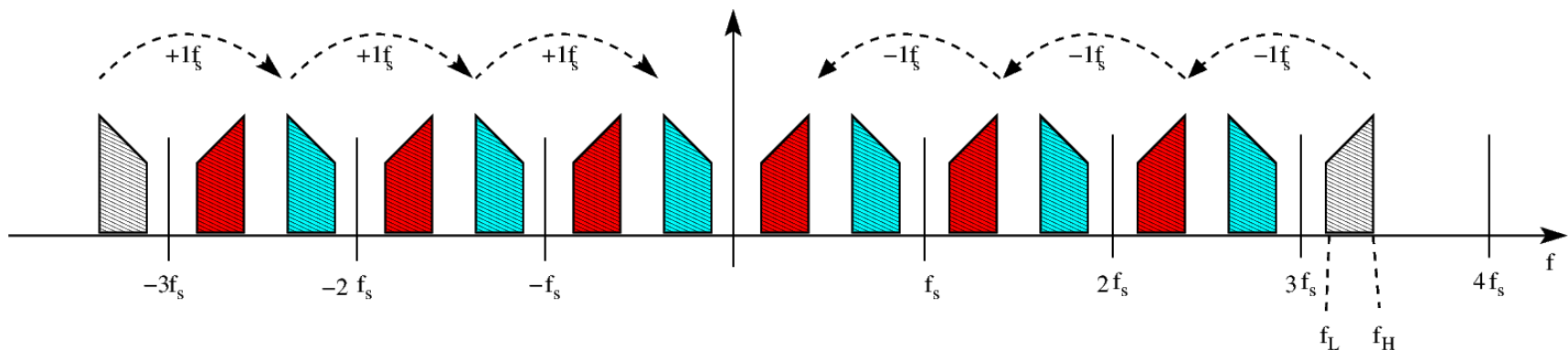
Sampling jitter problem: present with Nyquist sampling, much sharper with bandpass sampling. (steeper slope of the signal at the sampling point...)

Bandpass sampling - frequency choice

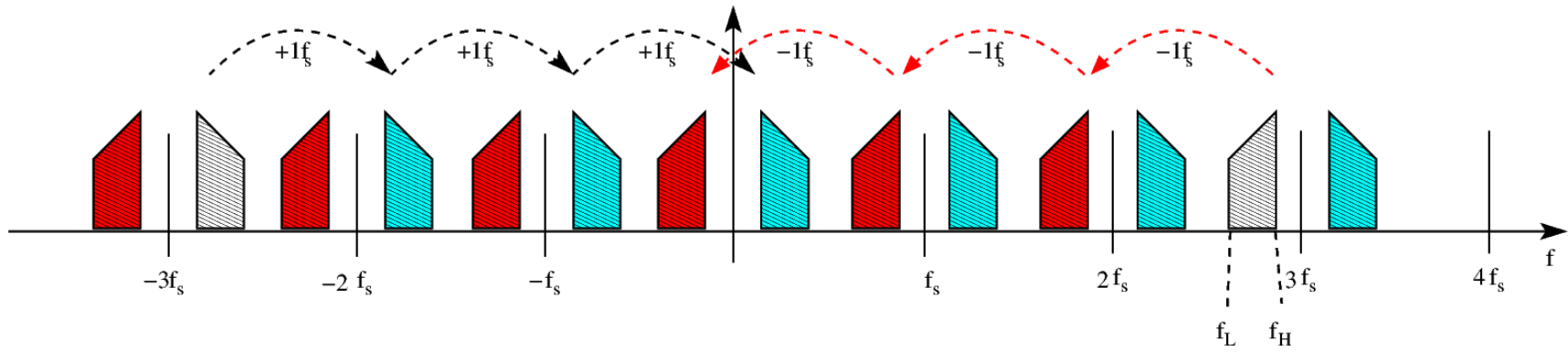
Signal frequency from f_L to f_H . (Assume real-valued signals, so actually from $-f_H$ to $-f_L$ and from f_L to f_H).

Bandwidth $B = f_H - f_L$ (one-sided...)

- Baseband sampling: $f_L \geq 0$, $f_H < f_s/2$
- N times undersampling $N \leq \frac{f_H}{B}$
- Avoid aliasing: $f_s \frac{N}{2} \geq f_H$, $f_s \frac{N-1}{2} \leq f_L$
- N even - spectrum mirroring!

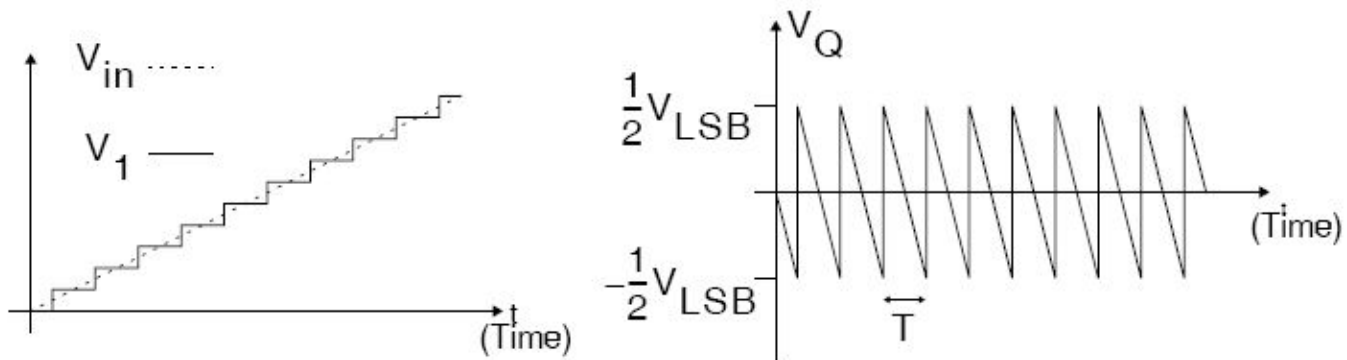
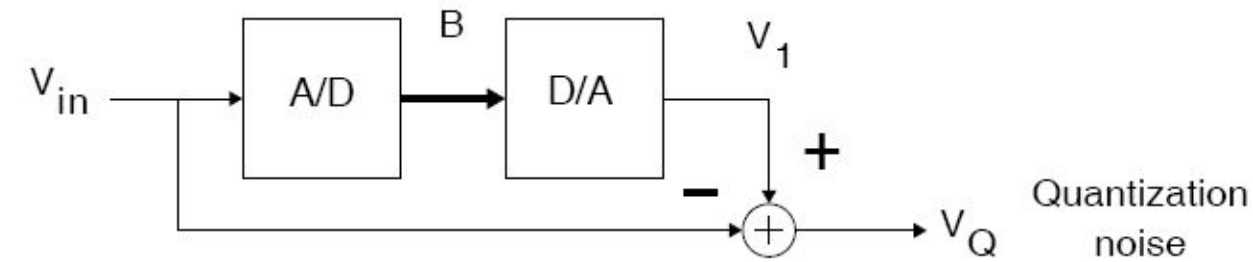


Bandpass sampling - mirroring



A/D noise

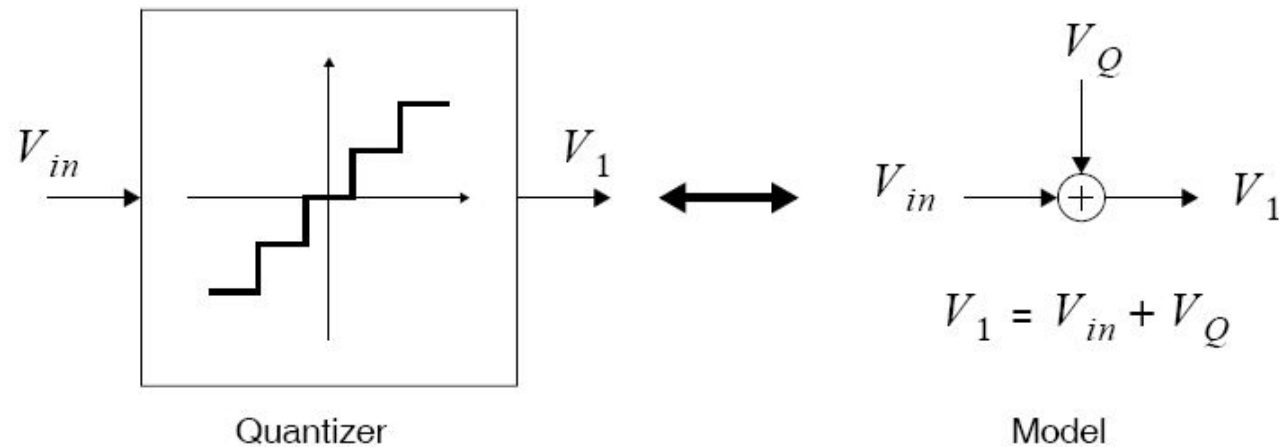
Quantization Noise



$$V_Q = V_1 - V_{in} \quad \text{or} \quad V_1 = V_{in} + V_Q \quad (8)$$

A/D noise

Quantization Noise



- Above model is exact
— approx made when assumptions made about V_Q
- Often assume V_Q is white, uniformly distributed
number between $\pm V_{\text{LSB}}/2$

A/D SNR

Noise amplitude: $q/2$, assumed uniformly distributed $\longrightarrow \sigma_n^2 = \frac{q^2}{12}$ (power).

Each extra bit gives 2x smaller q \longrightarrow 6.02 dB less noise.

SNR with assumption that “signal” is a maximum-amplitude ($V_{pp} = 2^N \cdot q$, and $power(\text{sinusoid}) = (V_{pp}/2)^2/2$) sinusoid:

$$\begin{aligned} SNR &= 10 \log_{10} \frac{\text{signal power}}{\text{noise power}} [dB] = 10 \log_{10} \frac{(2^N q)^2 / (2 \cdot 2^2)}{q^2 / 12} [dB] = \\ &= 10 \log_{10} (1.5 * 4^N) [dB] = 1.76 + 6.02 \cdot N [dB] \end{aligned}$$

Oversampling

- More space for transition band of antialiasing filter (A/D) or reconstruction filter (D/A)
 - (AD) later we may LP filter and downsample signal: we gain 1 bit of accuracy for a 4-sample average; more gain with *noise shaping* → sigma-delta converters (not discussed further at ESPTR)
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A/D types

- Multimeters: integrating (e.g. dual slope) = voltage to time conversion + time measurement
 - Slow signals: ramp voltage or successive approximation (D/A + comparator + control circuit)
 - Audio: usually sigma-delta (oversampling with 1/bit conversion and noise shaping + LP filter + decimation)
 - Video: flash (a ref voltage ladder + a lot of comparators)
 - Combo: subranging converter = more stages (rough AD + DA + next AD on the remainder)
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D/A and A/D problems

- speed
 - bits (from 6 to 24) - remember that this may be noise-limited or q limited...
 - nonidealities
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