

ESPTR: Radar Basics

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Prototype



RADAR - echolocation

RAdio Detection And Ranging

detection → transmit some energy and watch it return

ranging → and measure the round-trip time

Electromagnetic version

1865 James Clerk Maxwell - theory of electromagnetic waves

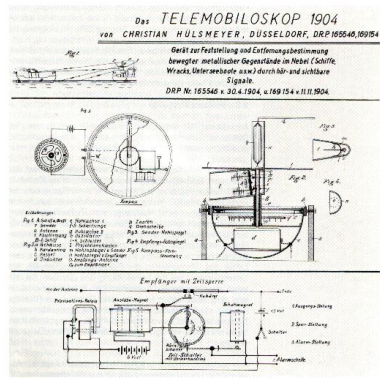
1886 Heinrich Hertz - experimental proof

1904 Christian Hülsmeyer - *Telemobiloskop*: ship collision avoidance apparatus, patented in Germany and UK; demonstration at the Rhine river in Cologne, DE.

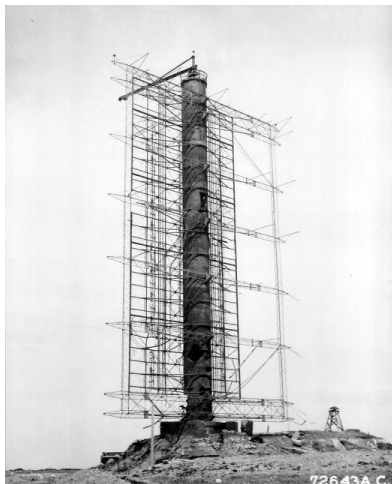
...

1939-1945 Chain Home, Klein Heidelberg and other installations

Telemobiloskop



Klein Heidelberg Parasit



Range 400 km, accuracy 1 - 2 km and 1 degree

Radar equation

Transmit-reflect-receive-detect:

<http://commons.wikimedia.org/wiki/File:Radarsops.gif>

Received power: radar *range* equation

$$P_r = \frac{P_t G_t A_r \sigma F^4}{(4\pi)^2 R_t^2 R_r^2}$$

P_t transmitter power

G_t gain of the transmitting antenna $G = 4\pi A_{\text{eff}}/\lambda^2$

A_r effective aperture (area) of the receiving antenna

σ radar cross section, or scattering coefficient, of the target

F pattern propagation factor

R_t distance from the transmitter to the target

R_r distance from the target to the receiver.

2x range $\rightarrow 2^4 = 16$ x power needed ...

Signal model

Transmit:

$$x_T(t) = A_T(t)e^{j\phi_T(t)}$$

Receive:

$$x_R(t) = A_T(t - R(t)/c)e^{j\phi_T(t - R(t)/c)}$$

simple case: $\phi_T(t) = \omega t + \phi_M(t)$, $R(t) = R_0 + vt$

$$x_R(t) = A_T(t - R_0/c - vt/c)e^{j(\omega(t - R_0/c - vt/c) + \phi_M(t - R_0/c - vt/c))}$$

$$x_R(t) = A_T(t - R_0/c - vt/c)e^{j(\omega t)} e^{-j\omega(R_0/c)} e^{-j\omega vt/c} e^{j\phi_M(t - R_0/c - vt/c)}$$

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Baseband:

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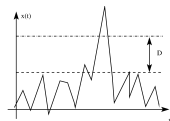
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Detection



→ compare signal with threshold

$$P_r > P_{noise} \cdot D \quad \longrightarrow \quad \text{declare a target}$$

with integration (by a matched filter) over t_i seconds

$$\frac{P_t G_t A_r \sigma F^4 t_i B}{(4\pi)^2 R_t^2 R_r^2} > kTBD$$

so the minimum detected object RCS

$$\sigma_{min} = \frac{(4\pi)^2 R_t^2 R_r^2 kTD}{P_t G_t A_r \sigma F^4 t_i}$$

We sometimes express σ in dBsm (dB w.r.t. square meter).

Detection threshold

$x(t) < D \longrightarrow H_0$ Hypothesis 0: only noise

$x(t) > D \longrightarrow H_1$ Hypothesis 1: noise + signal

Maximize P_d (detection), keep P_{fa} (false alarm) low.

The threshold D set above:

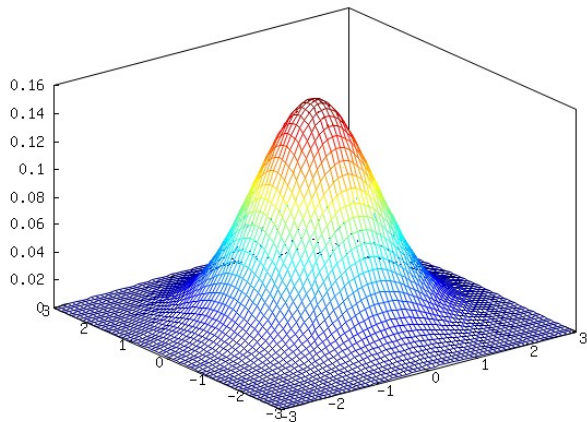
- ▶ Noise (thermal etc)
- ▶ Clutter (unwanted echoes)
- ▶ Multipath
- ▶ Jamming (intentionally malicious transmitters)
- ▶ Interferences (other equipment, e.g. other radars)

Improvements: matched filter ($S \uparrow$), interference cancellation ($C \downarrow$)

Typical: SNR ≈ 13 dB

Adaptation: CFAR

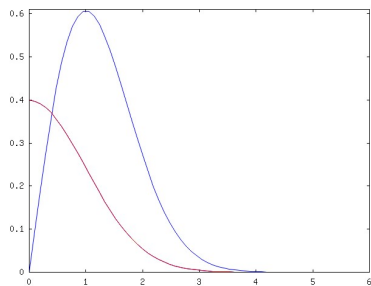
H0: Noise distribution (complex)



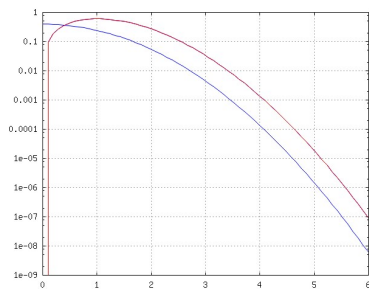
Two-dimensional (imag / real) gaussian distribution

H0: Noise distribution (abs)

$\text{abs}(\text{gaussian} + j * \text{gaussian}) = \text{rayleigh}$



lin scale

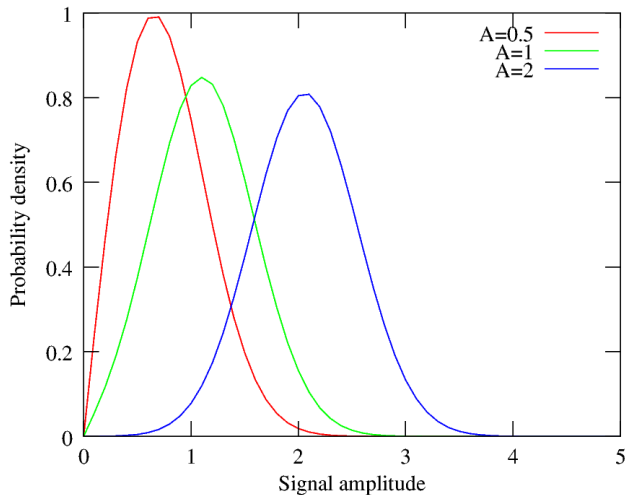


log scale

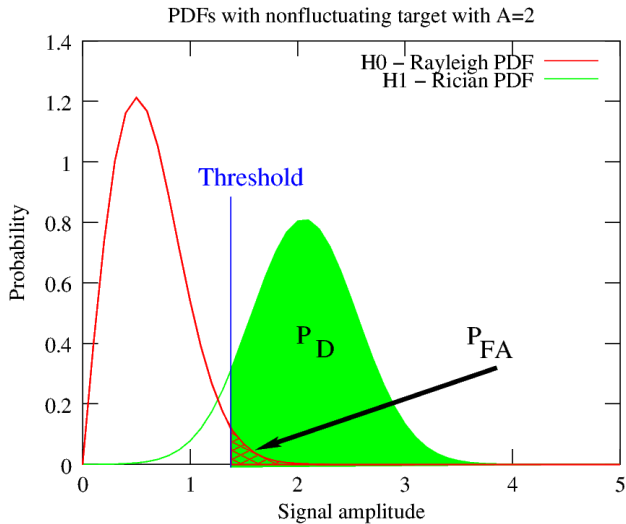
H1: Signal + noise distribution (abs)

$\text{abs}((\text{gaussian} + j * \text{gaussian}) + \text{constant } A) = \text{rician}$

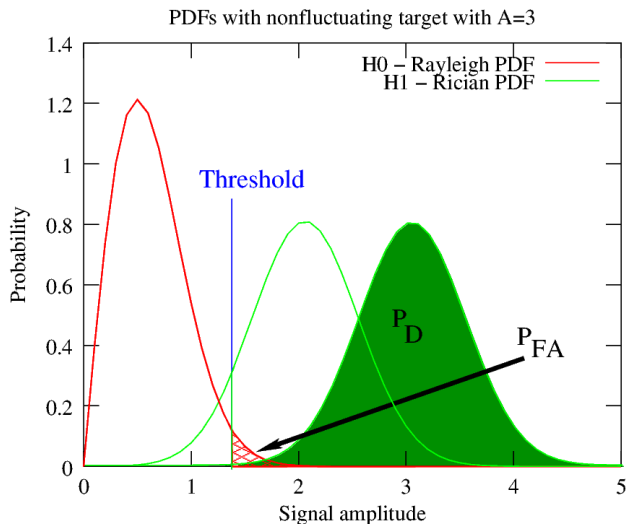
Rician PDF with $s=0.5$



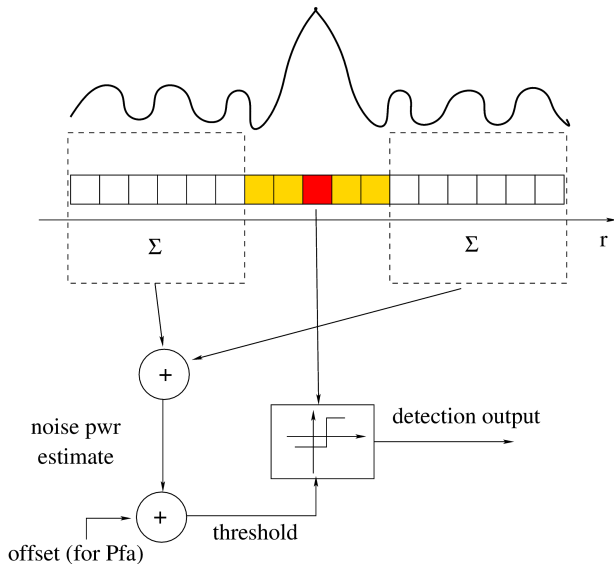
Neyman-Pearson detector



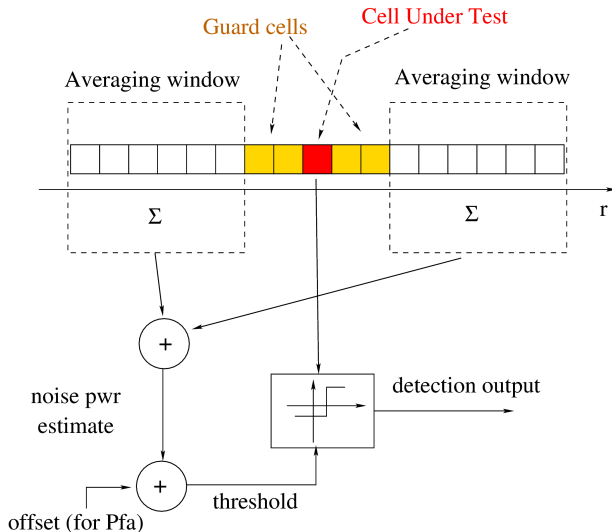
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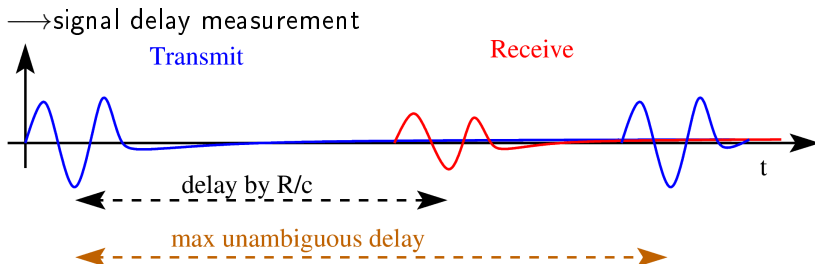
CFAR- Constant False Alarm Rate



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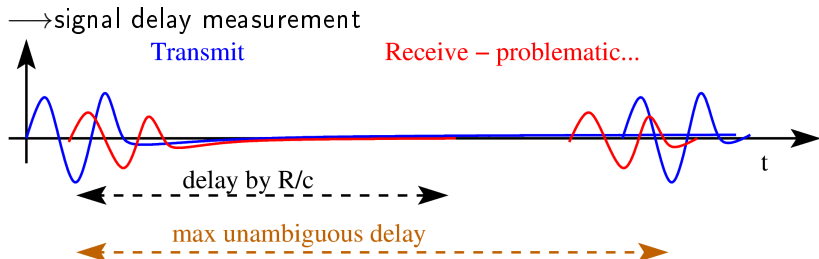


Range measurement



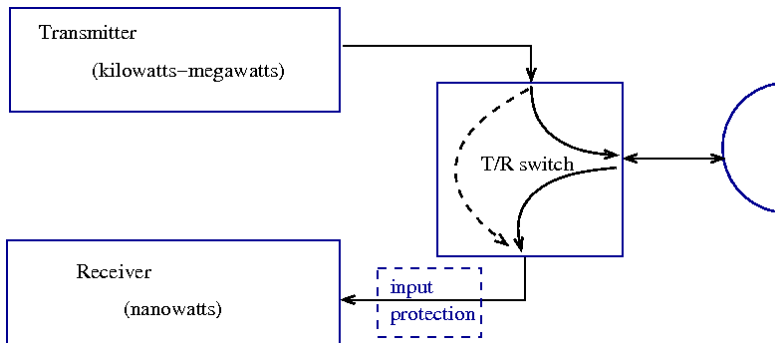
- ▶ Max *unambiguous* range limited by modulation period
- ▶ Min range limited by transmit signal entering the receiver (in pulsed radar)
 - ▶ Antenna separation
 - ▶ T/R switch + receiver safety (ionised gas + pin diode)

Range measurement



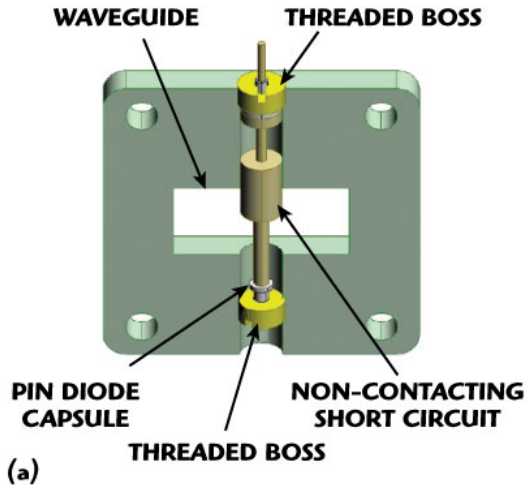
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Transmit/receive switch



Make friends with good microwave engineers ...

Receiver input protection



Velocity measurement

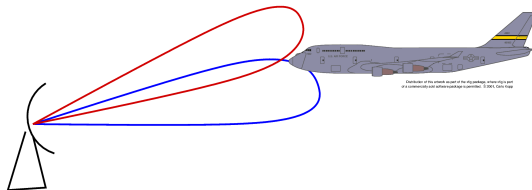


→ Doppler shift measurement

$$x_R(t) = A_T(t - R_0/c - vt/c) e^{j\phi_M(R_0/c + vt/c)} e^{j(\omega t)} e^{-j\omega(R_0/c)} e^{-j\omega vt/c}$$

- ▶ Min velocity: ground/meteo clutter
- ▶ Max velocity (frequency): inverse of modulation period (PRI)

Angle measurement



- ▶ azimuth
- ▶ elevation

Methods

- ▶ Scanning: mechanical, electronic
- ▶ Monopulse techniques (multielement antenna)
 - ▶ Power ratio
 - ▶ Sigma-Delta (power)
 - ▶ Phased arrays